

BSEH Practice Paper (March 2024)

(2023-24)

Marking Scheme MATHEMATICS

SET-B
CODE: 835

⇒ Important Instructions: • All answers provided in the Marking scheme are SUGGESTIVE
• Examiners are requested to accept all possible alternative correct answer(s).

SECTION – A (1Mark × 20Q)		
Q. No.	EXPECTED ANSWERS	Marks
Question 1.	Let R be the relation in the set N given by $R = \{(a, b) : b = a + 1, b > 5\}$. Choose the correct answer.	
Solution:	(B) $(7, 8) \in R$	1
Question 2.	$\cos^{-1}(\cos \frac{7\pi}{6})$ is equal to	
Solution:	(B) $\frac{5\pi}{6}$	1
Question 3.	If $A = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$, then $A'A$ is:	
Solution:	(A) I	1
Question 4.	If A and B are invertible matrices, then which of the following is not correct	
Solution:	(D) $(A + B)^{-1} = B^{-1} + A^{-1}$	1
Question 5.	If the vertices of a triangle are $(-2, -3)$, $(3, 2)$ and $(-1, -8)$, then by using determinants its area is	
Solution:	(A) 15	1
Question 6.	If $y = \log x^2$, then $\frac{d^2y}{dx^2}$ is equal to :	
Solution:	(A) $\frac{-2}{x^2}$	1
Question 7.	The antiderivative of $(1 - x)\sqrt{x}$ equals:	
Solution:	(B) $\frac{2}{3}x^{\frac{3}{2}} - \frac{2}{5}x^{\frac{5}{2}} + C$	1
Question 8.	$\int e^x \sec x (1 + \tan x) dx$ equals	
Solution:	(C) $e^x \sec x + C$	1
Question 9.	The value of $\int_{-\pi/2}^{\pi/2} \tan^5 x dx$ is	
Solution:	(C) 0	1
Question 10.	The degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^2 + \sin\left(\frac{dy}{dx}\right) + 1 = 0$ is :	

Solution:	(D) not defined	1
Question 11.	How many number of arbitrary constants are there in the general solution of a differential equation of fourth order?	
Solution:	4	1
Question 12.	The function $f(x) = \begin{cases} \frac{\sin x}{x} + \cos x, & \text{if } x \neq 0 \\ k, & \text{if } x = 0 \end{cases}$ is continuous at $x = 0$, then find the value of k	
Solution:	$\lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \left(\frac{\sin x}{x} + \cos x \right)$ $= 1 + 1$ $= 2$ <p>Since $f(x)$ is continuous at $x = 0$</p> $\therefore \lim_{x \rightarrow 0} f(x) = f(0)$ $\Rightarrow 2 = k$	1
Question 13.	If a line makes angles $90^\circ, 135^\circ, 45^\circ$ with the x, y and z-axes respectively, find its direction cosines.	
Solution:	<p>Line makes angles $90^\circ, 135^\circ, 45^\circ$ with the x,y and z-axes respectively</p> <p>\therefore Direction Cosines are</p> $l = \cos 90^\circ, m = \cos 135^\circ, n = \cos 45^\circ$ $l = 0, m = \frac{-1}{\sqrt{2}}, n = \frac{1}{\sqrt{2}}$ $\Rightarrow \text{D.C.'s are } < 0, \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >$	1
Question 14.	If $P(A) = \frac{3}{5}$ and $P(B) = \frac{1}{5}$, find $P(A \cap B)$ if A and B are independent events.	
Solution:	<p>Since A and B are independent therefore $P(A \cap B) = P(A) \cdot P(B)$</p> $\therefore P(A \cap B) = \frac{3}{5} \times \frac{1}{5} = \frac{3}{25}$	1
Question 15.	\vec{a} and $-\vec{a}$ are collinear. (True / False)	
Solution:	True	1
Question 16.	The probability of obtaining an even prime number on each die, when a pair of dice is rolled is $\frac{6}{36}$. (True / False)	
Solution:	False	1
Question 17.	If A and B are any two events such that $P(A) + P(B) - P(A \cap B) = P(A)$, then $P(A B)$ ____.	
Solution:	1	1
Question 18.	The projection vector of $\vec{a} = \hat{i} + 3\hat{j} + 7\hat{k}$ on $\vec{b} = 7\hat{i} - \hat{j} + 8\hat{k}$ is ____.	

[illegible]

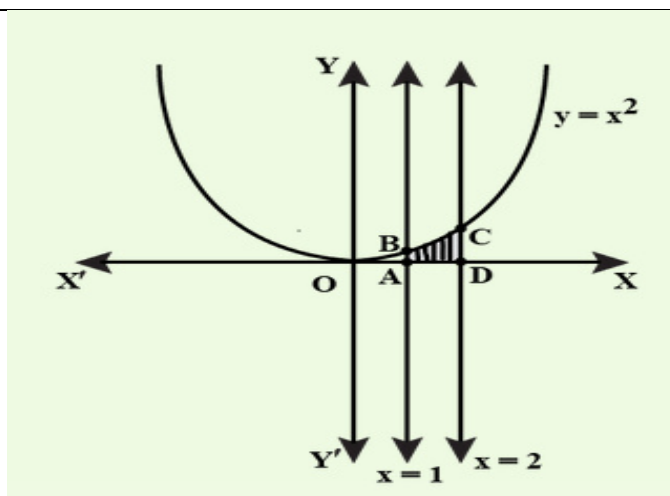
	$\frac{dy}{y \log y} = \frac{dy}{x} \quad \dots(1)$ <p>Integrating both sides of equation (1), we get</p> $\int \frac{dy}{y \log y} = \int \frac{dy}{x}$ $\log \log y = \log x + C$ <p>which is the general solution of equation (1)</p>	$\frac{1}{2}$ $1\frac{1}{2}$
Question 25.	An urn contains 10 black and 5 white balls. Two balls are drawn from the urn one after the other without replacement. What is the probability that both drawn balls are black?	
Solution:	<p>Total number of balls = 10 black balls + 5 red balls = 15 balls</p> <p>Let A be the event of drawing a black ball in first draw and B be the events of drawing a black ball in second draw.</p> <p>$P(A)$ = Probability of getting a black ball in the first draw = $\frac{10}{15} = \frac{2}{3}$</p> <p>As the ball is not replaced after the first throw,</p> <p>$\therefore P(B/A)$ = Probability of getting another black ball in the second draw = $\frac{8}{14} = \frac{4}{7}$</p> <p>Since the two balls are drawn without replacement, the two draws are not independent.</p> <p>$P(\text{both balls are black}) = P(A) \times P(B/A)$</p> <p>Now, the probability of getting both balls red = $\frac{2}{3} \times \frac{4}{7} = \frac{8}{21}$</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1
	SECTION – C (3Marks × 8Q)	
Question 26.	Let R be a relation on the set A of ordered pairs of positive integers defined by $(x, y) R (u, v)$ if and only if $xv = yu$. Show that R is an equivalence relation.	
Solution:	Clearly, $(x, y) R (x, y)$, $\forall (x, y) \in A$	

	<p>Since $xy = yx$ This shows that R is reflexive.</p> <p>Further, $(x, y) R (u, v)$ $\Rightarrow xv = yu$ $\Rightarrow uy = vx$ $\Rightarrow (u, v) R (x, y)$ This shows that R is symmetric.</p> <p>Similarly, $(x, y) R (u, v)$ and $(u, v) R (a, b)$ $\Rightarrow \begin{matrix} xv = yu & \text{and} & ub = va \\ \frac{x}{y} = \frac{u}{v} & \text{and} & \frac{u}{v} = \frac{a}{b} \\ \frac{x}{y} = \frac{a}{b} \\ \Rightarrow xb = ya \end{matrix}$ Hence $(x, y) R (a, b)$ Thus, R is transitive. Thus, R is an equivalence relation.</p>	<p>1</p> <p>1</p> <p>1</p>
OR Question 26.	Prove that: $\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}$	
Solution:	<p>$\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}$</p> <p>We know $\cos^{-1} x = \sin^{-1} \sqrt{1 - x^2}$ where $x < 1$</p> $\Rightarrow \cos^{-1} \frac{12}{13} = \sin^{-1} \sqrt{1 - \left(\frac{12}{13}\right)^2}$ $\Rightarrow = \sin^{-1} \sqrt{\frac{25}{169}}$ $\Rightarrow \cos^{-1} \frac{12}{13} = \sin^{-1} \frac{5}{13}$ <p>Now taking L.H.S. $= \sin^{-1} \frac{5}{13} + \sin^{-1} \frac{3}{5}$</p> <p>We know that,</p> $\sin^{-1} x + \sin^{-1} y = \sin^{-1} \left[x\sqrt{1 - y^2} + y\sqrt{1 - x^2} \right] \quad \text{if } xy < 1$ $\therefore = \sin^{-1} \left[\frac{5}{13} \sqrt{1 - \left(\frac{3}{5}\right)^2} + \frac{3}{5} \sqrt{1 - \left(\frac{5}{13}\right)^2} \right]$ $= \sin^{-1} \left[\frac{5}{13} \sqrt{\frac{16}{25}} + \frac{3}{5} \sqrt{\frac{144}{169}} \right]$ $= \sin^{-1} \left[\frac{5}{13} \left(\frac{4}{5}\right) + \frac{3}{5} \left(\frac{12}{13}\right) \right] = \sin^{-1} \frac{56}{65}$ <p>L.H.S. = R.H.S.</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$1\frac{1}{2}$</p>

	$y \cdot \frac{1}{\cos x}(-\sin x) + \log(\cos x) \cdot \frac{dy}{dx} = x \cdot \frac{1}{\cos y}(-\sin y) \cdot \frac{dy}{dx} + \log(\cos y) \cdot 1$ $-y \cdot (\tan x) + \log(\cos x) \cdot \frac{dy}{dx} = -x \cdot (\tan y) \cdot \frac{dy}{dx} + \log(\cos y)$ $(\log(\cos x) + x(\tan y)) \cdot \frac{dy}{dx} = \log(\cos y) - y \cdot (\tan x)$ $\frac{dy}{dx} = \frac{\log(\cos y) - y \cdot (\tan x)}{\log(\cos x) + x \cdot (\tan y)}$	$\frac{1}{2}$ $\frac{1}{2}$
Question 29.	Find the intervals in which the function f is given by $(x) = -2x^3 - 9x^2 - 12x + 1$ is strictly increasing or strictly decreasing.	
Solution:	<p>Given function: $f(x) = -2x^3 - 9x^2 - 12x + 1$</p> $f'(x) = -6x^2 - 18x - 12 = -6(x^2 + 3x + 2)$ $f'(x) = -6(x + 2)(x + 1), \dots\dots(1)$ <p>Now for increasing or decreasing, $f'(x) = 0$ $-6(x + 2)(x + 1) = 0$ $x + 2 = 0$ or $x + 1 = 0$ $x = -2$ or $x = -1$ Therefore, we have sub-intervals are $(-\infty, -2)$, $(-2, -1)$ and $(-1, \infty)$</p> <p>For interval $(-\infty, -2)$, picking $x = -3$, from equation (1), $f'(x) = (-ve)(-ve)(-ve) = (-ve) < 0$ Therefore, f is strictly decreasing in $(-\infty, -2)$</p> <p>For interval $(-2, -1)$, picking $x = -1.5$, from equation (1), $f'(x) = (-ve)(+ve)(-ve) = (+ve) > 0$ Therefore, f is strictly increasing in $(-2, -1)$.</p> <p>For interval $(-1, \infty)$, picking $x = 4$, from equation (1), $f'(x) = (-ve)(+ve)(+ve) = (-ve) < 0$ Therefore, f is strictly decreasing in $(-1, \infty)$. So, f is strictly decreasing in $(-\infty, -2)$ and $(-1, \infty)$. f is strictly increasing in $(-2, -1)$.</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
Question 30.	Integrate: $\int \frac{4x+1}{\sqrt{2x^2+x-3}} dx$	
Solution:	It is given that $I = \int \frac{4x+1}{\sqrt{2x^2+x-3}} dx$	

	<p>Here form of integral is $\int \frac{px+q}{\sqrt{ax^2+bx+c}} dx$</p> <p>$\therefore 4x + 1 = A \frac{d}{dx}(2x^2 + x - 3) + B$</p> <p>$4x + 1 = A(2x + 1) + B \quad \dots(1)$</p> <p>On comparing the like terms , we have</p> <p>$2A = 4 \quad \text{and} \quad A + B = 1$</p> <p>$\Rightarrow A = 2 \quad \text{and} \quad B = -1$</p> <p>$\Rightarrow 4x + 1 = 2(4x + 1) - 1 \quad \dots\text{from (1)}$</p> <p>$I = \int \frac{2(4x+1)-1}{\sqrt{2x^2+x-3}} dx$</p> <p>$I = 2 \int \frac{4x+1}{\sqrt{2x^2+x-3}} dx - \int \frac{1}{\sqrt{2x^2+x-3}} dx$</p> <p>Put $2x^2 + x - 3 = t \Rightarrow (4x + 1) dx = dt$</p> <p>$I = 2 \int \frac{1}{\sqrt{t}} dt - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x - \frac{3}{2}}} dx$</p> <p>$I = 4\sqrt{t} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x - \frac{3}{2}}} dx$</p> <p>$I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x + \frac{1}{4} - \frac{1}{4} - \frac{3}{2}}} dx \quad (\text{completing the square})$</p> <p>$I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{\left(x + \frac{1}{2}\right)^2 - \left(\frac{\sqrt{7}}{4}\right)^2}} dx$</p> <p>$I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \log \left \left(x + \frac{1}{2}\right) + \sqrt{\left(x + \frac{1}{2}\right)^2 - \left(\frac{\sqrt{7}}{4}\right)^2} \right + C$</p> <p>$I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \log \left \frac{(2x+1) + \sqrt{2x^2+x-3}}{2} \right + C$</p>	1
OR Question 30.	Evaluate: $\int_2^8 x - 5 dx$	
Solution:	<p>$I = \int_2^8 x - 5 dx$</p> <p>We know $x - 5 = \begin{cases} -(x - 5), & x \leq 5 \\ (x - 5), & x > 5 \end{cases}$</p> <p>$I = \int_2^5 x - 5 dx + \int_5^8 x - 5 dx$</p> <p>$I = \int_2^5 -(x - 5) dx + \int_5^8 (x - 5) dx$</p>	$\frac{1}{2}$

	$\vec{a}_1 = -\hat{i} - \hat{j} - \hat{k}, \quad \text{and} \quad \vec{b}_1 = 7\hat{i} - 6\hat{j} + \hat{k}$ $\vec{a}_2 = 3\hat{i} + 5\hat{j} + 7\hat{k} \quad \text{and} \quad \vec{b}_2 = \hat{i} - 2\hat{j} + \hat{k}$ <p>Therefore $\vec{a}_2 - \vec{a}_1 = 4\hat{i} + 6\hat{j} + 8\hat{k}$</p> <p>And $\vec{b}_1 \times \vec{b}_2 = (7\hat{i} - 6\hat{j} + \hat{k}) \times (\hat{i} - 2\hat{j} + \hat{k})$</p> $= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 7 & -6 & 1 \\ 1 & -2 & 1 \end{vmatrix} = -4\hat{i} - 6\hat{j} - 8\hat{k}$ $ \vec{b}_1 \times \vec{b}_2 = \sqrt{16 + 36 + 64} = \sqrt{116}$ <p>Hence, the shortest distance between the given lines is given by</p> $D = \frac{ (\vec{a}_2 - \vec{a}_1) \cdot (\vec{b}_1 \times \vec{b}_2) }{ \vec{b}_1 \times \vec{b}_2 } = \frac{ (4\hat{i} + 6\hat{j} + 8\hat{k}) \cdot (-4\hat{i} - 6\hat{j} - 8\hat{k}) }{\sqrt{116}}$ $\frac{ -16 - 36 - 64 }{\sqrt{116}} = \frac{116}{\sqrt{116}} = \sqrt{116} = 2\sqrt{29}$	$\frac{1}{2}$ $\frac{1}{2}$ 1 1
OR Question 33.	Find the vector equation of the line passing through the point $(1, -2, -3)$ and perpendicular to the two lines : $\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{3}$ and $\frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}$.	
Solution:	<p>The vector equation of a line passing through a point with position vector \vec{a} and parallel to \vec{b} is $\vec{r} = \vec{a} + \lambda \vec{b}$.</p> <p>It is given that, the line passes through $(1, -2, -3)$ So, $\vec{a} = 1\hat{i} - 2\hat{j} - 3\hat{k}$</p> <p>Given lines are $\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{3}$ and $\frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}$</p> <p>It is also given that, line is perpendicular to both given lines. So we can say that the line is perpendicular to both parallel vectors of two given lines.</p>	1



1

Required area is shaded region ABCD:

$$|\int_1^2 y \, dx| = |\int_1^2 x^2 \, dx| \quad [\text{From equation (1)}]$$

$$= \left| \frac{\mathbf{x}^3}{3} \right|_1^2$$

$$= \frac{1}{3} |(2^3 - 1^3)|$$

$$= \frac{1}{3} |(8 - 1)| = \frac{1}{3} (7) = \frac{7}{3} \text{ sq. units}$$

2

OR
Question 34.

Find the area of the region bounded by the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$

Solution:

Here $\frac{x^2}{4} + \frac{y^2}{9} = 1$... (1)

It is a vertical ellipse having center at origin and is symmetrical about both axes (if we change y to $-y$ or x to $-x$, equation remain same).

Standard equation of an ellipse is $\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$

By comparing, $a = 3$ and $b = 2$

From equation (1)

$$\Rightarrow y^2 = \frac{9}{4} (4 - x^2)$$

$$\Rightarrow y = \frac{3}{2} \sqrt{4 - x^2} \quad \dots\dots(2)$$

Points of Intersections of ellipse (1) with x-axis ($y = 0$)

Put $y = 0$ in equation (1), we have

$$\frac{1}{2}$$

1

$$x^2/4 = 1 \Rightarrow x^2 = 4$$

$$\Rightarrow x = \pm 2$$

Therefore, Intersections of ellipse(1) with x-axis are (0, 2) and (0, -2).

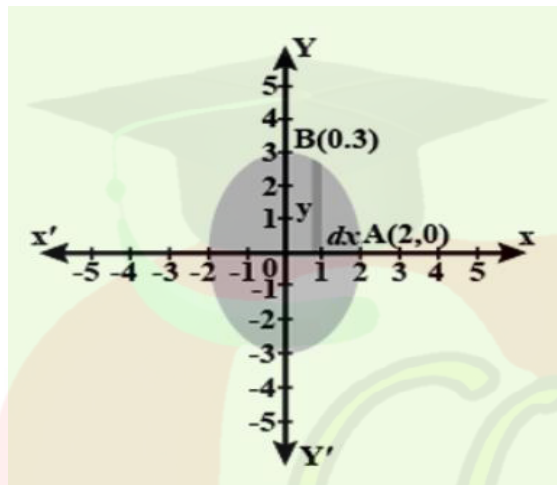
Points of Intersections of ellipse (1) with y-axis (x = 0)

$$\text{Putting } x = 0 \text{ in equation (1), } y^2/9 = 1 \Rightarrow y^2 = 9$$

$$\Rightarrow y = \pm 3.$$

Therefore, Intersections of ellipse (1) with y-axis are (0, 3) and (0,-3).

for arc of ellipse in first quadrant.



Now,

Area of region bounded by ellipse (1)

Total shaded area = 4 x Area OAB of ellipse in first quadrant

$$= 4 \left| \int_0^2 y \cdot dx \right| \quad [\because \text{at end B of arc AB of ellipse: } x=0 \text{ and at end A of arc AB; } x=2]$$

$$= 4 \left| \int_0^2 \frac{3}{2} \sqrt{4 - x^2} \cdot dx \right| = 6 \left| \int_0^2 \sqrt{2^2 - x^2} \cdot dx \right|$$

$$= 6 \left[\frac{x}{2} \sqrt{2^2 - x^2} + \frac{2^2}{2} \sin^{-1} \frac{x}{2} \right]_0^2 \quad [\because \int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a}]$$

$$= 6 \left[\left(\frac{2}{2} \sqrt{4 - 4} + 2 \sin^{-1} 1 \right) - (0 + 2 \sin^{-1} 0) \right] = 6 \left[0 + \left(2 \frac{\pi}{2} \right) \right]$$

$$= 6\pi \text{ sq. Units}$$

1

$\frac{1}{2}$

$1\frac{1}{2}$

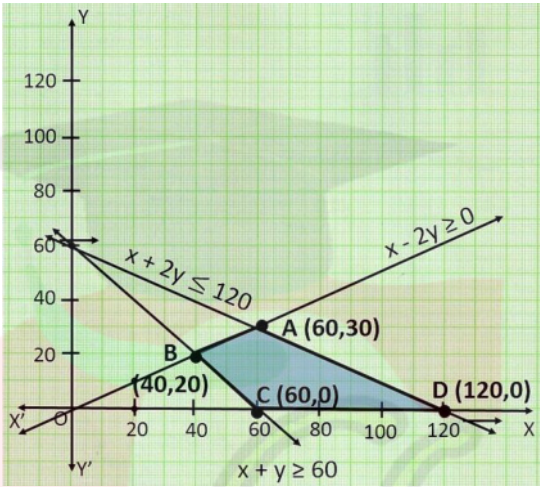
$\frac{1}{2}$

Question 35.	Solve the following problem graphically: Minimise and Maximise $Z = 5x + 10y$ Subject to the constraints: $x + 2y \leq 120$ $x + y \geq 60$ $x - 2y \geq 0$ $x \geq 0, y \geq 0$																	
Solution:	$Z = 5x + 10y$(1) $x + 2y \leq 120$...(2) $x + y \geq 60$(3) $x - 2y \geq 0$...(4) $x \geq 0, y \geq 0$...(5) First of all, let us graph the feasible region of the system of linear inequalities (2) to (5). Let $Z = 5x + 10y$(1) Converting inequalities to equalities $x + 2y = 120$ <table border="1"><tr><td>X</td><td>0</td><td>120</td></tr><tr><td>Y</td><td>60</td><td>0</td></tr></table> Points are (0, 60), (120,0) Now put (0, 0) in inequation (2), we find $0 \leq 120$, which is true. Therefore area lies towards the origin from this line. $x + y = 60$ <table border="1"><tr><td>x</td><td>0</td><td>60</td></tr><tr><td>y</td><td>60</td><td>0</td></tr></table> Points are (0, 60), (60, 0) Now put (0, 0) in inequation (3), we find $0 \geq 60$, which is False. Therefore area lies away from the origin from this line. $x - 2y = 0$ <table border="1"><tr><td>X</td><td>0</td><td>20</td><td>40</td></tr></table>	X	0	120	Y	60	0	x	0	60	y	60	0	X	0	20	40	$\frac{1}{2}$ <
X	0	120																
Y	60	0																
x	0	60																
y	60	0																
X	0	20	40															

y	0	10	20
---	---	----	----

Points are (0,0),(20,10),(40,20)
 Now put (1, 0) in inequation (4),
 we find $1 \geq 0$, which is true.
 Therefore area lies towards (1, 0) origin from this line.

Plot the graph for the set of points



To find maximum and minimum
 The feasible region ABCD is shown in the figure. Note that the region is bounded. The coordinates of the corner points A, B, C and D are (60, 30), (40, 20), (60, 0) and (120, 0) respectively.

Corner Point	Corresponding Value of $Z = 5x + 10y$
A (60, 30)	600←Maximum
B (40, 20)	400
C (60, 0)	300←Minimum
D (120, 0)	600←Maximum (Multiple optimal solutions)

We now find the minimum and maximum value of Z.
 From the table, we find that the minimum value of Z is 300 at the point B (60, 0) of the feasible region.

	The maximum value of Z on the feasible region occurs at the two corner points C (60, 30) and D (120, 0) and it is 600 in each case.	$\frac{1}{2}$
	SECTION – E (4Marks × 3Q)	
Question 36.	<p>$P(x) = -6x^2 + 120x + 25000$ (in ₹) is the total profit function of a company, where x denotes the production of the company.</p> <p>Based on the above information answer the following:</p> <p>(i) Find the profit of the company when the production is 3 units. (1)</p> <p>(ii) Find $P'(5)$. (1)</p> <p>(iii) Find the production, when the profit is maximum. (2)</p>	
Solution:	<p>(i) When $x = 3$ $P(3) = -6(3)^2 + 120(3) + 25000$ $= -54 + 360 + 25000$ $= ₹ 25306$</p>	1
	<p>(ii) We have, $P(x) = -6x^2 + 120x + 25000$... (1) Differentiating equation (1) w.r.t. x $P'(x) = -12x + 120$... (2) $\therefore P'(5) = -12(5) + 120 = 60$</p>	1
	<p>(iii) We have, $P(x) = -6x^2 + 120x + 25000$... (1) Differentiating equation (1) w.r.t. x $P'(x) = -12x + 120$... (2) For maximum or minimum value of $P(x)$, $P'(x) = 0$ we have $-12x + 120 = 0$ $-12x = -120$ i.e. $x = 10$ Differentiating equation (2) w.r.t. x $P''(x) = -12$ Now , At $x = 10$ $P''(x) = -12 = -ve$ $\Rightarrow P(x)$ has maximum value at $x = 10$</p>	2
Question 37.	<p>A linear differential equation is of the form $\frac{dy}{dx} + Py = Q$, where P, Q are functions of x, then such equation is known as linear differential equation. Its solution is given by $y \cdot (I.F.) = \int Q(I.F.) dx + c$, where I.F.(Integrating Factor) = $e^{\int P dx}$ Now, suppose the given equation is $x \frac{dy}{dx} + 2y = x^2$ Based on the above information, answer the following questions:</p>	

	<p>(i)What are the values of P and Q respectively? (1)</p> <p>(ii)What is the value of I.F.? (1)</p> <p>(iii)Find the Solution of given equation. (2)</p>	
Solution:	<p>(i) Given equation is $x \frac{dy}{dx} + 2y = x^2$ Dividing on both side by x, we have $\frac{dy}{dx} + \frac{2}{x} y = x$ $\Rightarrow P = \frac{2}{x}, Q = x$</p>	1
	<p>(ii) I.F.(Integrating Factor) = $e^{\int P dx}$ $= e^{\int \frac{2}{x} dx}$ $= e^{2 \log x}$ $= x^2$</p>	1
	<p>(iii) Solution of given equation is $y \cdot (IF.) = \int Q(IF.) dx + c$ $y(x^2) = \int x(x^2) dx + c$ $x^2 y = \int x^3 dx + c$ $x^2 y = \frac{x^4}{4} + c$</p>	2
Question 38.	<p>In an office three employees Vinay, Sonia and Iqbal process incoming copies of a certain form. Vinay process 50% of the forms. Sonia processes 20% and Iqbal the remaining 30% of the forms. Vinay has an error rate of 0.06, Sonia has an error rate of 0.04 and Iqbal has an error rate of 0.03. <i>Based on the above information answer the following questions:</i></p>	

	<p>(i) The total probability of committing an error in processing the form. (2)</p> <p>(ii) The manager of the company wants to do a quality check. During inspection he selects a form at random from the days output of processed forms. If the form selected at random has an error, the probability that the form is not processed by Vinay. (2)</p>	
Solution:	<p>(i) Let E_1 = Event of processing form by Vinay. E_2 = Event of processing form by Soniya. E_3 = Event of processing form by Iqbal.</p> $P(E_1) = \frac{50}{100} = \frac{5}{10}, \quad P(E_2) = \frac{20}{100} = \frac{2}{10}, \quad P(E_3) = \frac{30}{100} = \frac{3}{10}$ <p>Also $P(A/E_1) = 0.06, \quad P(A/E_2) = 0.04, \quad P(A/E_3) = 0.03$</p> <p>Required Probability</p> $ \begin{aligned} P(A) &= P(E_1) \cdot P(A/E_1) + P(E_2) \cdot P(A/E_2) + P(E_3) \cdot P(A/E_3) \\ &= \frac{5}{10} (0.06) + \frac{2}{10} (0.04) + \frac{3}{10} (0.03) \\ &= 0.03 + 0.008 + 0.009 = 0.047 \end{aligned} $	2
	<p>(ii) Probability that the form is not processed by Vinay = $P(\bar{E}_1 A)$ $P(\bar{E}_1 A) = 1 - P(E_1 A)$</p> <p>By Bayes' Theorem</p> $P(E_1 A) = \frac{P(E_1) \cdot P(A/E_1)}{P(E_1) \cdot P(A/E_1) + P(E_2) \cdot P(A/E_2) + P(E_3) \cdot P(A/E_3)}$ $P(E_1 A) = \frac{\frac{5}{10} (0.06)}{0.047}$ $P(E_1 A) = \frac{0.03}{0.047} = \frac{30}{47}$ $P(\bar{E}_1 A) = 1 - P(E_1 A)$ $= 1 - \frac{30}{47} = \frac{17}{47}$	2